

Scheda di allenamento:
Sistemi di Disequazioni di 1° grado
Risoluzione e rappresentazione grafica

1. Sistemi di primo grado (Livello Base)

Parte Base 1. *Risolvi i seguenti sistemi di disequazioni:*

1. ■□□ $\begin{cases} x + 4 > 0 \\ x - 2 > 0 \end{cases}$ [$x > 2$]

2. ■□□ $\begin{cases} 2x \leq 10 \\ x + 1 \geq 0 \end{cases}$ [$-1 \leq x \leq 5$]

3. ■□□ $\begin{cases} x - 1 < 0 \\ x - 5 > 0 \end{cases}$ [*impossibile*]

4. ■□□ $\begin{cases} 3x \leq 9 \\ x + 2 > 0 \end{cases}$ [$-2 < x \leq 3$]

5. ■□□ $\begin{cases} x < 4 \\ x > 6 \end{cases}$ [*impossibile*]

6. ■□□ $\begin{cases} 2x - 4 > 0 \\ x - 5 < 0 \end{cases}$ [$2 < x < 5$]

7. ■□□ $\begin{cases} \frac{1}{2}x < \frac{3}{2} \\ x + 3 > 0 \end{cases}$ [$-3 < x < 3$]

8. ■□□ $\begin{cases} 1 - x < 3 \\ x + 4 < 4 \end{cases}$ [$-2 < x < 0$]

9. ■□□ $\begin{cases} x - 2 > 0 \\ x - 8 > 0 \end{cases}$ [$x > 8$]

10. ■□□ $\begin{cases} 5x + 10 < 0 \\ 4x \geq 0 \end{cases}$ [*impossibile*]

11. ■□□ $\begin{cases} x + 5 < 0 \\ 2x < 4 \end{cases}$ [$x < -5$]

12. ■□□ $\begin{cases} 2x + 8 < 0 \\ x - 1 < 0 \end{cases}$ $[x < -4]$
13. ■□□ $\begin{cases} x - 3 > 0 \\ 10 - x > 0 \end{cases}$ $[3 < x < 10]$
14. ■□□ $\begin{cases} x + 4 > 0 \\ 2x \leq 6 \end{cases}$ $[-4 < x \leq 3]$
15. ■□□ $\begin{cases} 6x \leq 18 \\ x + 5 > 0 \end{cases}$ $[-5 < x \leq 3]$
16. ■□□ $\begin{cases} x + 2 > 2 \\ x - 1 < 0 \end{cases}$ $[0 < x < 1]$
17. ■□□ $\begin{cases} 4x - 8 \geq 0 \\ x - 5 < 0 \end{cases}$ $[2 \leq x < 5]$
18. ■□□ $\begin{cases} x + 6 > 0 \\ 3 - x \geq 0 \end{cases}$ $[-6 < x \leq 3]$
19. ■□□ $\begin{cases} 2x < 10 \\ x + 1 > 5 \end{cases}$ $[4 < x < 5]$
20. ■□□ $\begin{cases} x - 7 \leq 0 \\ x + 2 \geq 0 \end{cases}$ $[-2 \leq x \leq 7]$

2. Sistemi di tre disequazioni lineari - Livello base

$$21. \blacksquare\square\square \begin{cases} x + 5 > 0 \\ x - 1 < 0 \\ x \geq -2 \end{cases} \quad [-2 \leq x < 1]$$

$$22. \blacksquare\square\square \begin{cases} 3x > 6 \\ x < 10 \\ x - 4 > 0 \end{cases} \quad [4 < x < 10]$$

$$23. \blacksquare\square\square \begin{cases} x + 1 \geq 0 \\ 6 - x > 0 \\ x < 4 \end{cases} \quad [-1 \leq x < 4]$$

$$24. \blacksquare\square\square \begin{cases} x - 3 < 0 \\ x + 1 > 0 \\ 2x \geq 0 \end{cases} \quad [0 \leq x < 3]$$

$$25. \blacksquare\square\square \begin{cases} x > -4 \\ x \leq 5 \\ x - 2 < 0 \end{cases} \quad [-4 < x < 2]$$

$$26. \blacksquare\square\square \begin{cases} x \geq 0 \\ x < 8 \\ x + 2 > 5 \end{cases} \quad [3 < x < 8]$$

$$27. \blacksquare\square\square \begin{cases} x - 1 < 10 \\ x + 4 > 0 \\ x < 5 \end{cases} \quad [-4 < x < 5]$$

$$28. \blacksquare\square\square \begin{cases} 2x \geq 0 \\ x - 5 \leq 0 \\ x + 1 > 1 \end{cases} \quad [0 < x \leq 5]$$

$$29. \blacksquare\square\square \begin{cases} x + 6 > 0 \\ x - 4 < 0 \\ 5x < 10 \end{cases} \quad [-6 < x < 2]$$

$$30. \blacksquare\square\square \begin{cases} x - 2 \geq 0 \\ x \leq 10 \\ x + 1 > 4 \end{cases} \quad [3 < x \leq 10]$$

$$31. \blacksquare \square \square \quad \begin{cases} x + 3 > 0 \\ x - 5 < 0 \\ x \geq 0 \end{cases} \quad [0 \leq x < 5]$$

$$32. \blacksquare \square \square \quad \begin{cases} 2x > 4 \\ x < 10 \\ x - 1 > 0 \end{cases} \quad [2 < x < 10]$$

$$33. \blacksquare \square \square \quad \begin{cases} x + 2 \geq 0 \\ 8 - x > 0 \\ x < 5 \end{cases} \quad [-2 \leq x < 5]$$

$$34. \blacksquare \square \square \quad \begin{cases} x - 4 \leq 0 \\ x + 1 > 0 \\ 3x \geq 0 \end{cases} \quad [0 \leq x \leq 4]$$

$$35. \blacksquare \square \square \quad \begin{cases} x > -1 \\ x \leq 6 \\ x - 3 < 0 \end{cases} \quad [-1 < x < 3]$$

$$36. \blacksquare \square \square \quad \begin{cases} x + 10 > 0 \\ x - 4 \leq 0 \\ 2x \geq -2 \end{cases} \quad [-1 \leq x \leq 4]$$

$$37. \blacksquare \square \square \quad \begin{cases} 3x < 15 \\ x + 2 > 0 \\ x \geq 1 \end{cases} \quad [1 \leq x < 5]$$

$$38. \blacksquare \square \square \quad \begin{cases} x - 5 < 0 \\ x + 4 > 0 \\ x \leq -6 \end{cases} \quad [\emptyset]$$

$$39. \blacksquare \square \square \quad \begin{cases} x + 7 \geq 0 \\ x < 2 \\ 1 - x \leq 0 \end{cases} \quad [1 \leq x < 2]$$

$$40. \blacksquare \square \square \quad \begin{cases} x > -10 \\ x < 0 \\ 3x + 9 > 0 \end{cases} \quad [-3 < x < 0]$$

3. Sistemi di disequazioni avanzati

Parte Avanzata 1. Risolvi i seguenti sistemi di disequazioni di livello avanzato:

$$41. \blacksquare\blacksquare\blacksquare \quad \begin{cases} \frac{x-1}{2} - \frac{2x(x+1)}{3} < \frac{1-2x^2}{3} + 1 \\ \frac{2}{3}(x - \frac{1}{4}) + \frac{1}{6} - (x-1)(x+1) \leq 1 - x^2 \end{cases} \quad [-11 < x \leq 0]$$

$$42. \blacksquare\blacksquare\blacksquare \quad \begin{cases} \frac{1}{3}(x + 2 - \frac{x+5}{2}) < \frac{x+4}{5} - \frac{x+3}{4} \\ 4[(4x-1)^2 + x] + (6x-1)^2 \leq 4x + (10x-1)^2 \end{cases} \quad [\frac{1}{6} \leq x < 1]$$

$$43. \blacksquare\blacksquare\blacksquare \quad \begin{cases} (2-x)(x+1) + \frac{(x+2)^2}{3} > x \cdot \frac{3-2x}{3} + x + 2 \\ \frac{x+1}{5} - 3(2x+1) < \frac{3-2x}{2} + \frac{1}{2} \end{cases} \quad [x > -1]$$

$$44. \blacksquare\blacksquare\blacksquare \quad \begin{cases} 4(\frac{1}{8}x - 2) - \frac{x}{4} \leq -\frac{x+3}{3} \\ \frac{1}{3}x + 2 > \frac{1}{2}x - \frac{x-5}{6} + 1 \end{cases} \quad [x \leq 12]$$

$$45. \blacksquare\blacksquare\blacksquare \quad \begin{cases} 5x + 1 \leq -2(x - 11) \\ 4 - 4x > 11 \\ x - 3 > -(1 - x) \end{cases} \quad [impossibile]$$

$$46. \blacksquare\blacksquare\blacksquare \quad \begin{cases} \frac{x-1}{2} - \frac{x+1}{3} \leq 1 - \frac{x}{6} \\ (x-2)(x+2) > (x-1)^2 - 5 \end{cases} \quad [0 < x \leq \frac{11}{2}]$$

$$47. \blacksquare\blacksquare\blacksquare \quad \begin{cases} (x+3)^2 - x^2 < 2x + 10 \\ \frac{x-1}{2} - \frac{x-2}{3} \geq \frac{1}{6} \end{cases} \quad [0 \leq x < \frac{1}{4}]$$

$$48. \blacksquare\blacksquare\blacksquare \quad \begin{cases} (x-1)^3 - x^2(x-3) < 4x + 5 \\ \frac{2x-1}{3} \geq x - 1 \end{cases} \quad [-6 < x \leq 2]$$

$$49. \blacksquare\blacksquare\blacksquare \quad \begin{cases} \frac{1}{2}(x-2)^2 \leq \frac{x^2+4}{2} - x \\ (x+1)^2 - (x-1)^2 > 4 \end{cases} \quad [x > 1]$$

$$50. \blacksquare\blacksquare\blacksquare \quad \begin{cases} \frac{x-3}{4} - \frac{x+1}{2} < \frac{1-x}{8} \\ (x-1)(x+3) \geq x^2 - 4 \end{cases} \quad [x \geq -\frac{1}{2}]$$

$$51. \blacksquare\blacksquare\blacksquare \quad \begin{cases} (x-1)^3 - x(x+2)^2 + 7x^2 \leq 5x + 2 \\ \frac{x-1}{3} - \frac{x+2}{2} > -2 \end{cases} \quad [-\frac{1}{2} \leq x < 4]$$

$$52. \blacksquare\blacksquare\blacksquare \quad \begin{cases} \frac{(2x+1)^2}{4} - x(x-2) \geq \frac{1}{4} \\ (x+2)^2 - (x-1)^2 < 15 \end{cases} \quad [0 \leq x < 2]$$

$$53. \blacksquare\blacksquare\blacksquare \quad \begin{cases} (x-1)(x^2 + x + 1) - x^3 < 2x - 5 \\ \frac{1}{2}x - \frac{x-3}{4} \leq 1 \end{cases} \quad [\emptyset]$$

54. ■■■■
$$\begin{cases} \frac{(x-2)(x+2)}{3} - \frac{x^2-1}{3} \geq x - 2 \\ 5x - 2(x - 3) < 12 \end{cases} \quad [x \leq 1]$$
55. ■■■■
$$\begin{cases} (x + 2)^3 - x^2(x + 6) > 12x + 5 \\ \frac{2x+3}{2} - \frac{3x-1}{4} \geq 1 \end{cases} \quad [x \geq -3]$$
56. ■■■■
$$\begin{cases} \frac{x-1}{4} - \frac{2x-3}{2} \geq \frac{x}{8} \\ (x + 2)^2 - (x - 1)^2 < 15 \end{cases} \quad [x \leq \frac{10}{7}]$$
57. ■■■■
$$\begin{cases} \frac{1}{3}(x - 1)(x + 1) - \frac{x^2-3}{3} \geq \frac{x-2}{2} \\ 4x - 2(x - 3) < 10 \end{cases} \quad [x < 2]$$
58. ■■■■
$$\begin{cases} (x - 1)^3 - x^2(x - 3) \leq 4x + 5 \\ \frac{2x-1}{3} \geq x - 1 \end{cases} \quad [-6 \leq x \leq 2]$$
59. ■■■■
$$\begin{cases} \frac{x+2}{3} - \frac{2x-1}{4} > \frac{x}{12} \\ (x + 1)^2 - x(x + 2) \leq 5 \end{cases} \quad [x < \frac{11}{3}]$$
60. ■■■■
$$\begin{cases} \frac{(x-2)^2}{2} - \frac{x^2-4}{2} \leq x + 1 \\ 3(x + 1) - 2(x - 1) > 0 \end{cases} \quad [x \geq 1]$$
61. ■■■■
$$\begin{cases} (x + 1)^3 - x^2(x + 3) \leq 5x + 2 \\ \frac{x-1}{2} - \frac{2x-3}{3} > \frac{1}{6} \end{cases} \quad [-\frac{1}{2} \leq x < 2]$$
62. ■■■■
$$\begin{cases} \frac{2x+3}{2} - \frac{3x-1}{4} \geq 1 \\ (x - 2)^2 - (x + 1)^2 > -9 \end{cases} \quad [-3 \leq x < 2]$$
63. ■■■■
$$\begin{cases} (2x - 1)^2 - 4x(x + 2) \leq 5 \\ \frac{x-1}{3} - \frac{x+1}{2} > -1 \end{cases} \quad [-\frac{1}{3} \leq x < 1]$$
64. ■■■■
$$\begin{cases} \frac{x-1}{2} - \frac{2x+1}{3} < \frac{x}{6} \\ (x + 1)^3 - x(x^2 + 3x) \geq 4x - 1 \end{cases} \quad [-\frac{5}{2} < x \leq 2]$$
65. ■■■■
$$\begin{cases} \frac{x-2}{3} - \frac{x+2}{4} > \frac{x-10}{12} \\ 2(x - 3)^2 - 2x^2 + 12x \leq 18 \end{cases} \quad [impossibile]$$
66. ■■■■
$$\begin{cases} (x - 2)^3 - x(x - 3)^2 \leq 4 \\ \frac{2x-1}{4} - \frac{x+1}{3} < \frac{x-13}{12} \end{cases} \quad [x < -6]$$
67. ■■■■
$$\begin{cases} \frac{1}{2}(x + 1)^2 - \frac{1}{2}(x - 1)^2 \geq 3x - 1 \\ (x + 2)(x - 2) - (x - 3)^2 \leq 5 \end{cases} \quad [x \leq 1]$$
68. ■■■■
$$\begin{cases} \frac{(x-1)(x+1)}{2} - \frac{(x-2)^2}{2} > 3 \\ 4x - \frac{2x-1}{3} \leq 11 \end{cases} \quad [\frac{11}{4} < x \leq \frac{16}{5}]$$

$$69. \blacksquare\blacksquare\blacksquare \quad \begin{cases} (x+1)^3 - x^2(x+3) < 4x - 2 \\ \frac{x-1}{2} + \frac{x+1}{3} \geq \frac{5x-1}{6} \end{cases} \quad [x > 3]$$

$$70. \blacksquare\blacksquare\blacksquare \quad \begin{cases} \frac{x+1}{3} - \frac{x-1}{2} > 1 \\ x - \frac{x-2}{3} \leq 1 \end{cases} \quad [x < -1]$$

4. Sistemi di disequazioni letterali

Parte Avanzata 2. Risolvi i seguenti sistemi di disequazioni nell'incognita x , discutendo i risultati in base ai valori dei parametri reali:

$$71. \blacksquare\blacksquare\blacksquare \quad \begin{cases} ax < 3a \\ x + 2 > 0 \end{cases} \quad (\text{con } a \neq 0) \quad [a > 0, -2 < x < 3; a < 0, x > 3]$$

$$72. \blacksquare\blacksquare\blacksquare \quad \begin{cases} ax \geq a^2 \\ x < a + 1 \end{cases} \quad (\text{con } a \neq 0) \quad [a > 0, a \leq x < a + 1; a < 0, x \leq a]$$

$$73. \blacksquare\blacksquare\blacksquare \quad \begin{cases} bx > 2 \\ 2bx < 8 \end{cases} \quad (\text{con } b \neq 0) \quad [b > 0, \frac{2}{b} < x < \frac{4}{b}; b < 0, \frac{4}{b} < x < \frac{2}{b}]$$

$$74. \blacksquare\blacksquare\blacksquare \quad \begin{cases} x + m^2 > 0 \\ 2x - m^2 < 0 \end{cases} \quad [-m^2 < x < \frac{m^2}{2}]$$

$$75. \blacksquare\blacksquare\blacksquare \quad \begin{cases} a(x - 2) > a^2 \\ 3x < 3a + 12 \end{cases} \quad (\text{con } a \neq 0) \quad [a > 0, a + 2 < x < a + 4; a < 0, x < a + 2]$$

$$76. \blacksquare\blacksquare\blacksquare \quad \begin{cases} ax - a^2 > 0 \\ x - 2a < 0 \end{cases} \quad (\text{con } a \neq 0) \quad [se\ a > 0, a < x < 2a; se\ a < 0, 2a < x < a]$$

$$77. \blacksquare\blacksquare\blacksquare \quad \begin{cases} (k - 1)x \leq k^2 - 1 \\ x + 1 > 0 \end{cases} \quad (k \neq 1) \quad \left[\begin{array}{l} k > 1 \implies -1 < x \leq k + 1 \\ k < 1 \implies x \geq k + 1 \end{array} \right]$$

$$78. \blacksquare\blacksquare\blacksquare \quad \begin{cases} 2ax \geq 4a \\ x - a < 3 \end{cases} \quad (\text{con } a \neq 0) \quad [se\ a > 0, 2 \leq x < a + 3; se\ a < 0, disc.\ x]$$

$$79. \blacksquare\blacksquare\blacksquare \quad \begin{cases} mx - m \leq 0 \\ x + m^2 > 0 \end{cases} \quad (\text{con } m \neq 0) \quad [se\ m > 0, -m^2 < x \leq 1; se\ m < 0, x \geq 1]$$

$$80. \blacksquare\blacksquare\blacksquare \quad \begin{cases} a(x - 1) < a(2 - a) \\ x + a > 1 \end{cases} \quad (a \neq 0) \quad \left[\begin{array}{l} a > 0 \implies 1 - a < x < 3 - a \\ a < 0 \implies x > 3 - a \end{array} \right]$$